Name: $\qquad$

Read each question carefully before answering. Answer all parts. Show all work, calculations, and/or reasoning, otherwise no points will be awarded. Properly labeled loops must be shown on K-maps. Point values are as indicated.

1. (25 points) Given the following circuit diagram, fill out the timing diagram for $X, Y$ and $Z$. Each AND gate has a delay of 2 ns , and each OR gate has a delay of 1 ns .


2. (15 points) Using only 2 to 1 multiplexers, draw a circuit diagram for a 5 to 1 MUX. Include a truth table.
3. (20 points) Use a 4 to 1 MUX and a minimum number of external gates to realize the function $F(A, B, C, D)=\Sigma m(3,5,7,12,14)+\Sigma d(0,1,4,6,15)$. Draw a circuit diagram and write the corresponding MUX equation.

|  | $A B$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $C D$ | 00 | 01 | 11 | 10 |
| 00 |  |  |  |  |
| 01 |  |  |  |  |
| 11 |  |  |  |  |
| 10 |  |  |  |  |



$$
F=
$$

$\qquad$
4. (15 points) Use the following 4 to 16 decoder and a minimum number of external gates to realize the function $F(A, B, C, D)=\Sigma m(1,3,5,7,12,14)+\Sigma d(4,8,11,13)$. (In other words, draw the circuit diagram below using the decoder inputs and/or outputs.) Assume that you have access to gates with only two inputs.

5. (15 points) Fill out the following timing diagram for a falling-edge triggered $J K$ flip-flop. Ignore propagation delays. The value of $Q$ is initially equal to 1 .

6. (15 points) Fill out the following timing diagram for a rising-edge triggered $T$ flip-flop. Ignore propagation delays. The value of $Q$ is initially equal to 0 .

7. (30 points) Design a 3 -bit counter that counts in the sequence ( $001,101,010,110,000,011 \ldots$ ) using $T$ flip-flops and a minimum number of external gates. Determine the logic required on the input of each flip-flop, then draw the circuit diagram.

| $A$ | $B$ | $C$ | $A^{+}$ | $B^{+}$ | $C^{+}$ | $T_{A}$ | $T_{B}$ | $T_{C}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 |  |  |  |  |  |  |
| 0 | 0 | 1 |  |  |  |  |  |  |
| 0 | 1 | 0 |  |  |  |  |  |  |
| 0 | 1 | 1 |  |  |  |  |  |  |
| 1 | 0 | 0 |  |  |  |  |  |  |
| 1 | 0 | 1 |  |  |  |  |  |  |
| 1 | 1 | 0 |  |  |  |  |  |  |
| 1 | 1 | 1 |  |  |  |  |  |  |

